

Prob. 86 Interplanetary Navigation.

- a.) Earth to Mars: You must increase the speed of the rocket in the direction of the earth's motion.  
 Mars to Earth: You must decrease the speed of the rocket w.r.t. the direction of Mar's motion.

b.)  $T = \frac{2\pi}{\sqrt{GM_{Sun}}} a^{3/2}$  is the period of the full elliptical orbit where  $1/2$  of the orbit is shown in Fig. 12.37

So,  $\frac{T}{2} = \frac{\pi}{\sqrt{GM_{Sun}}} a^{3/2}$  where  $a = \frac{(d_{earth} + d_{mars})}{2} = \frac{1.50 \times 10^{11} + 2.28 \times 10^{11}}{2} = 1.89 \times 10^{11} \text{ m}$

$\frac{T}{2} = \frac{\pi (1.89 \times 10^{11})^{3/2}}{\sqrt{6.67 \times 10^{-11} (1.99 \times 10^{30})}}$        $\frac{T}{2} = 2.24 \times 10^7 \text{ s} = 259 \text{ days}$

c.) What angle does Mars subtend during 259 days.  
 The period of Mars  $\rightarrow T = \frac{2\pi}{\sqrt{GM}} a^{3/2} = \frac{2\pi (2.28 \times 10^{11})^{3/2}}{\sqrt{6.67 \times 10^{-11} (1.99 \times 10^{30})}} = 5.94 \times 10^7$

$T_{Mars} = 5.94 \times 10^7 \text{ sec}$

fraction =  $\frac{T/2}{T_{Mars}}$  ← from part (b) = 0.377

$0.377 \times 360^\circ = 136^\circ$  in 259 days

$\theta = 180^\circ - 136^\circ = \underline{\underline{44^\circ}}$

